



Rising 7th Grade Language Arts & Pre-Algebra Summer Assignments 2025

Language Arts

7th grade will select **one book** to read from the following list of books:

- *Esperanza Rising* – Pam Munoz Ryan
- *One for the Murphys* – Lynda Mullaly Hunt
- *War Horse* – Michael Morpurgo.

When students have finished reading, they need to create **3 different creative journal entries (pages)**. A creative journal entry is a notebook page with drawings and/or sketches along with the writing. Examples of creative journal entries are attached.

- Ideas include - setting, characters, plot, theme, and free-choice entries.
- Journal entries need to be completed on notebook paper and labeled.
- To receive full credit, each journal must include the following:
 - graphics with color
 - writing that includes text evidence
 - analysis (thought prompts)
- Entries should be detailed, thoughtful, and creative.



Students will submit their journals on the first day of school in August, worth 60 points. They should also bring their book to school for the first week, as we will be discussing the books in class.

Choice Reading: While students are only required to read one book, reading all summer long is encouraged. Choose novels that interest you and are on your reading level. It is good to challenge yourself a little! Remember, reading is the single most important factor in student success.

7th Grade Pre-Algebra

Summer math is assigned to help students retain math skills and enable the math classes to spend less time reviewing past material and forge ahead with new math skills. It has been designed to review topics students learned during the past school year, which are crucial for success in the next grade level.

All students are expected to complete the entire Summer Skills packet to the *best of their ability*. Students should show their work so we can see the thought process used to complete the

problems.  or  your final answer. We are looking for a *good effort* at completing the problems, more than a correct answer. This includes attempting the problems and showing the work/thought process used to achieve an answer. A pacing suggestion would be to complete 2 - 3 pages a week. **This assignment is due Wednesday, August 13th, the first day of the new school year, and is worth 50 points.**

Here's a list of highly recommended authors for middle school readers (grades 6–8), across genres and interests. These authors are known for engaging plots, relatable characters, and age-appropriate themes:

Realistic Fiction

- **Jason Reynolds** – *Ghost*, *Look Both Ways*
- **Sharon Draper** – *Out of My Mind*, *Blended*
- **Jacqueline Woodson** – *Brown Girl Dreaming*, *Harbor Me*
- **Gordon Korman** – *Restart*, *Ungifted*
- **R.J. Palacio** – *Wonder*

Historical Fiction

- **Ruta Sepetys** – *Between Shades of Gray*, *Salt to the Sea*
- **Lauren Tarshis** – *I Survived* series (accessible for younger or reluctant readers)
- **Alan Gratz** – *Refugee*, *Ground Zero*, *Prisoner B-3087*
- **Pam Muñoz Ryan** – *Esperanza Rising*, *Echo*

Fantasy / Science Fiction

- **Rick Riordan** – *Percy Jackson* series, *Heroes of Olympus*
- **Tamora Pierce** – *Song of the Lioness*, *The Circle of Magic*
- **Eoin Colfer** – *Artemis Fowl* series
- **Tui T. Sutherland** – *Wings of Fire* series
- **Brandon Mull** – *Fablehaven*, *Beyonders*

Mystery / Adventure

- **Stuart Gibbs** – *Spy School*, *FunJungle*
- **Trenton Lee Stewart** – *The Mysterious Benedict Society*
- **Jennifer Nielsen** – *The False Prince*, *Resistance*
- **Anthony Horowitz** – *Alex Rider* series

Graphic Novels

- **Raina Telgemeier** – *Smile*, *Drama*, *Guts*
- **Gene Luen Yang** – *American Born Chinese*, *Dragon Hoops*
- **Victoria Jamieson** – *Roller Girl*, *When Stars Are Scattered*
- **Jerry Craft** – *New Kid*, *Class Act*

Poetry / Novels in Verse

- **Kwame Alexander** – *The Crossover*, *Booked*
- **Nikki Grimes** – *Garvey's Choice*, *Bronx Masquerade*


7th and 8th Grade Samples

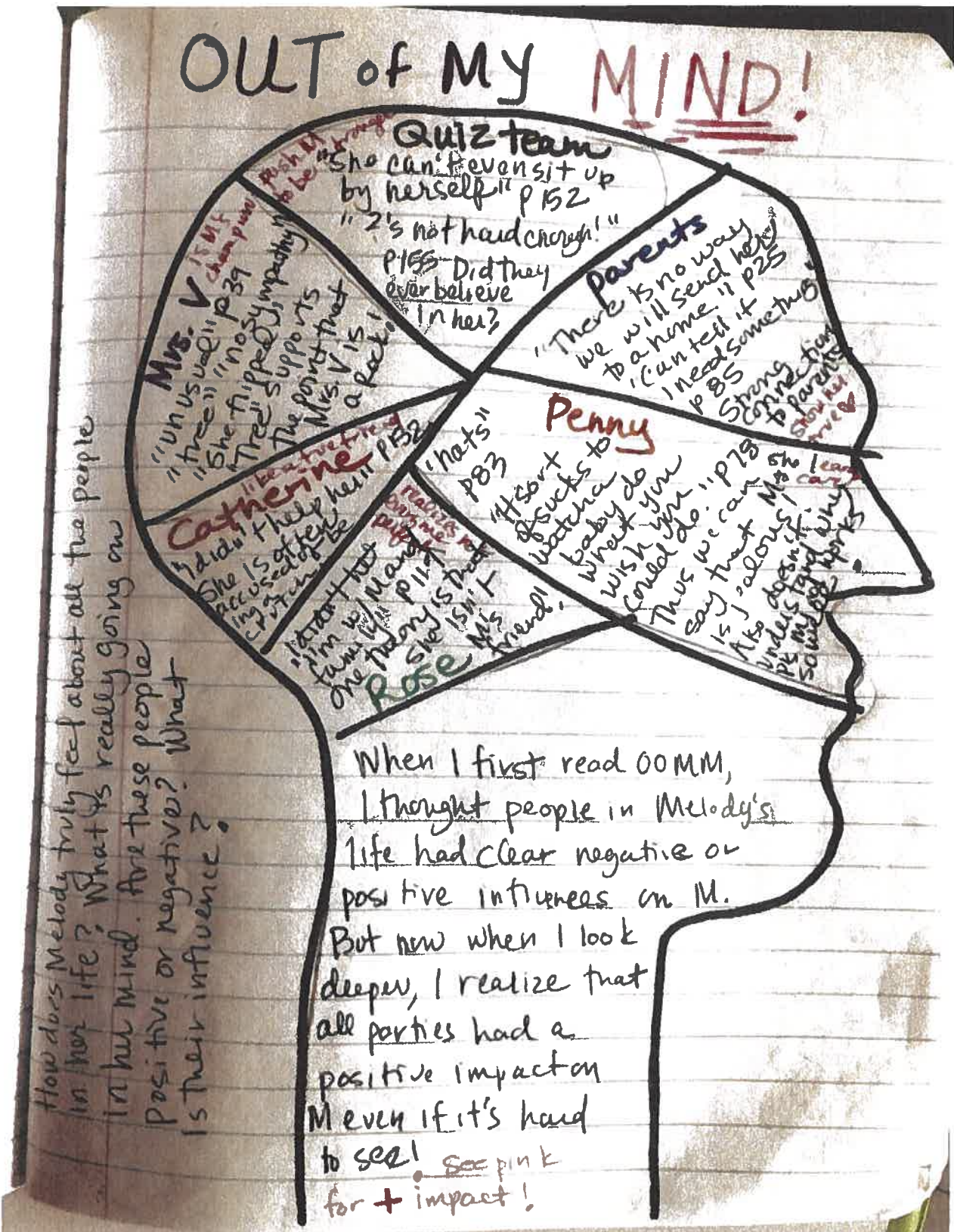
Comparing 2 characters:

	Rosa	Jessica
Both have Freedom	<ul style="list-style-type: none"> • philosophical • Hopeful • Kind • contained • trapped • smart 	<ul style="list-style-type: none"> • Kind • free • athletic • hopeful • happy

but, in different ways

Rosa and Jessica are very alike and different at the same time. They are similar in the physical way that they both have disabilities but, are different in the way they think and that Rosa is not free. One theory is that Rosa is such a philosophical thinker because she has been trapped in her mind. This is where she finds her freedom to roam pondering questions like "where does wind go?" Jessica though she has lost a leg is still free to roam in real life giving her not as much time to have internal thoughts like Rosa.





Symbolism: Chapters 16-19 4/17/16

Benin Home



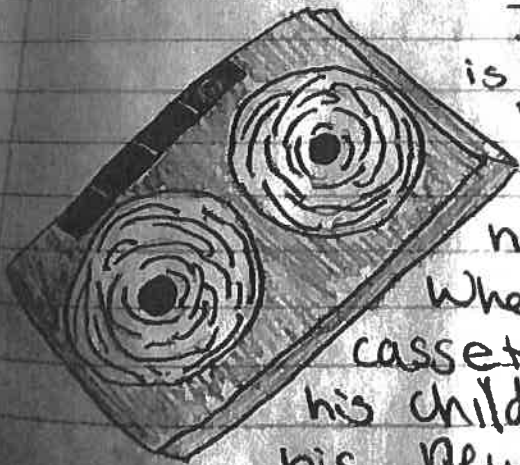
Benin Home symbolized Beah's life as a boy soldier ending. It tried to civilize the boys, however, you can take a boy out of a war, but you can't take the war out of a boy.

Esther

Esther symbolizes Beah's end to his psychological war. I believe this because every time Esther treated Beah, he would not tell her his name. However, on page 153 Beah finally opened up to Esther, by telling her his name. This shows Beah is finally learning how to trust people again, and forgive himself of what he has done.



Cassette



Ishmael Beah's cassette is a symbol of his childhood. For example, when Beah was little, music brought his brother and friends together. When the soldier threw Beah's cassette into the fire, it represented his childhood being destroyed and his new life as a boy soldier bein

Name: _____ Date: _____

Summer Reading Project

	Points Earned	Points Possible
Journal Entry #1		
• Color		3
• Graphics		3
• Text Evidence		7
• Thought Prompts/Analysis		7
Journal Entry #2		
• Color		3
• Graphics		3
• Text Evidence		7
• Thought Prompts/ Analysis		7
Journal Entry #3		
• Color		3
• Graphics		3
• Text Evidence		7
• Thought Prompts/Analysis		7
TOTAL		60

$\lim_{x \rightarrow 1} \frac{ctgx-2}{2\sqrt{1x^3}}$ $\int (x \pm a)^n dx = \frac{(x \pm a)^{n+1}}{n+1}$ $\frac{A-C}{C} = \lim_{x \rightarrow 1} \frac{ctgx-2}{2\sqrt{1x^3}}$ $\int (x \pm a)^n dx = \frac{(x \pm a)^{n+1}}{n+1}$ $\frac{A-C}{C} =$

$+y^2=Z$ $S_3 = \begin{bmatrix} 10 & 0 \\ 10 & 1 \\ 10 & 1 \end{bmatrix}$ $\phi = \sqrt{\sum (x-m)^2}$ $S_3 = \begin{bmatrix} 10 & 0 \\ 10 & 1 \\ 10 & 1 \end{bmatrix}$ $\phi = \sqrt{\sum (x-m)^2}$ $S = \int_2^5 5t dt$ $x = \frac{\Delta x}{\Delta z}$

$P = r^2 \pi$ $\Delta t = T - \frac{3}{x}$ $(x-y)^2$ $y=2$ $\int \frac{\sqrt{x+a^2}}{x} dx =$ $e =$ $P = \sum_{i=0}^{\infty} x_i^a$ $y =$ $= (y-1)^2$ $B \lim_{x \rightarrow 1} \frac{ctgx-2}{2\sqrt{1x^3}}$ $+y^2=Z$ $P = r^2 \pi$ $\Delta t = T - \frac{3}{x}$ $(x-y)^2$ $y=2$ $\int \frac{\sqrt{x+a^2}}{x} dx =$ $e =$ $P = \sum_{i=0}^{\infty} x_i^a$ $y =$ $= (y-1)^2$ $B \lim_{x \rightarrow 1} \frac{ctgx-2}{2\sqrt{1x^3}}$ $+y^2=Z$ $P = r^2 \pi$ $\Delta t = T - \frac{3}{x}$ $(x-y)^2$ $y=2$ $\int \frac{\sqrt{x+a^2}}{x} dx =$ $e = 2,79$ $\sim -\cos x + \tan y \tan(2a) - \frac{2 \tan(a)}{1 + \dots}$

RIISING 7TH GRADE

PRE-ALGEBRA

SUMMER MATH

PACKET

2025



1-2 Pre-Algebra Summer Skills**Words and Expressions**

Translate Verbal Phrases into Expressions A **numerical expression** contains a combination of numbers and operations such as addition, subtraction, multiplication, and division. Verbal phrases can be translated into numerical expressions by replacing words with operations and numbers.

+	-	×	÷
plus	minus	times	divide
the sum of	the difference of	the product of	the quotient of
Increased by	decreased by	of	divided by
more than	less than		among

Example

Write a numerical expression for each verbal phrase.

- a. the product of seventeen and three

Phrase the product of seventeen and three

Expression 17×3

- b. the total number of pencils given to each student if 18 pencils are shared among 6 students

Phrase 18 shared among 6

Expression $18 \div 6$

Exercises

Write a numerical expression for each verbal phrase.

- eleven less than twenty
- twenty-five increased by six
- sixty-four divided by eight
- the product of seven and twelve
- the quotient of forty and eight
- sixteen more than fifty-four
- six groups of twelve
- eighty-one decreased by nine

1-2 Pre-Algebra Summer Skills*(continued)***Words and Expressions**

Order of Operations Evaluate, or find the numerical value of, expressions with more than one operation by following the **order of operations**.

Step 1 Evaluate the expressions inside grouping symbols.

Step 2 Multiply and/or divide from left to right.

Step 3 Add and/or subtract from left to right.

Example Evaluate each expression.

a. $6 \cdot 5 - 10 \div 2$

$$\begin{aligned} 6 \cdot 5 - 10 \div 2 &= 30 - 10 \div 2 \\ &= 30 - 5 \\ &= 25 \end{aligned}$$

Multiply 6 and 5.

Divide 10 by 2.

Subtract 5 from 30.

b. $4(3 + 6) + 2 \cdot 11$

$$\begin{aligned} 4(3 + 6) + 2 \cdot 11 &= 4(9) + 2 \cdot 11 \\ &= 36 + 22 \\ &= 58 \end{aligned}$$

Evaluate $(3 + 6)$.

Multiply 4 and 9, and 2 and 11.

Add 36 and 22.

c. $3[(7 + 5) \div 4 - 1]$

$$\begin{aligned} 3[(7 + 5) \div 4 - 1] &= 3[12 \div 4 - 1] \\ &= 3(3 - 1) \\ &= 3(2) \\ &= 6 \end{aligned}$$

Evaluate $(7 + 5)$ first.

Divide 12 by 4.

Subtract 1 from 3.

Multiply 3 and 2.

Exercises

Evaluate each expression.

1. $6 + 3 \cdot 9$

2. $7 + 7 \cdot 3$

3. $14 - 6 + 8$

4. $26 - 4 + 9$

5. $10 \div 5 \cdot 3$

6. $22 \div 11 \cdot 6$

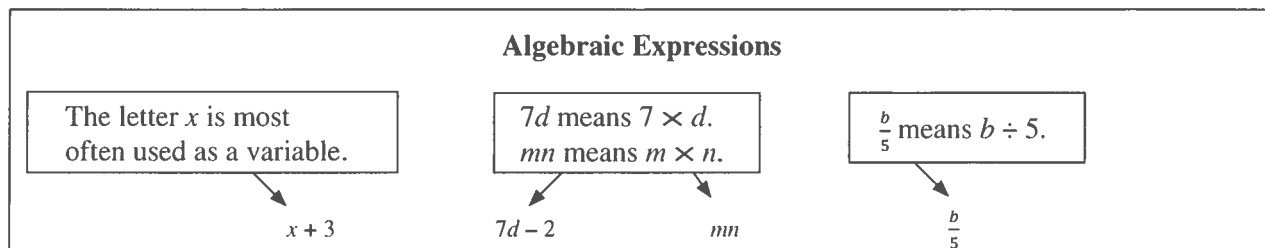
7. $2(6 + 2) - 4 \cdot 3$

8. $5(6 + 1) - 3 \cdot 3$

9. $2[(13 - 4) + 2(2)]$

1-3 Pre-Algebra Summer Skills***Variables and Expressions***

Translate Verbal Phrases An **algebraic expression** is a combination of variables, numbers, and at least one operation. A **variable** is a letter or symbol used to represent an unknown value. To translate verbal phrases with an unknown quantity into algebraic expressions, first define the variable.

**Example**

Translate each phrase into an algebraic expression.

- a. five inches longer than the length of a book**

Words five inches longer than the length of a book

Variable Let b represent the length of the book.

Expression $b + 5$

- b. two less than the product of a number and eight**

Words two less than the product of a number and eight

Variable Let n represent the unknown number.

Expression $8n - 2$

Exercises

Translate each phrase into an algebraic expression.

1. eight inches taller than Mycala's height
2. twelve more than four times a number
3. the difference of sixty and a number
4. three times the number of tickets sold
5. fifteen dollars more than a saved amount
6. the quotient of the number of chairs and four
7. a number of books less than twenty-three
8. five more than six times a number

1-3 Pre-Algebra Summer Skills *(continued)***Variables and Expressions**

Evaluate Expressions To evaluate an algebraic expression, replace the variable(s) with known values and follow the order of operations.

Substitution Property of Equality

Words If two quantities are equal, then one quantity can be replaced by the other.

Symbols For all numbers a and b , if $a = b$, then a may be replaced by b .

Example

ALGEBRA Evaluate each expression if $r = 6$ and $s = 2$.

a. $8s - 2r$

$$8s - 2r = 8(2) - 2(6)$$

Replace r with 6 and s with 2.

$$= 16 - 12 \text{ or } 4$$

Multiply. Then subtract.

b. $3(r + s)$

$$3(r + s) = 3(6 + 2)$$

Replace r with 6 and s with 2.

$$= 3 \cdot 8 \text{ or } 24$$

Evaluate the parentheses. Then multiply.

c. $\frac{5rs}{4}$

$$\frac{5rs}{4} = 5rs \div 4$$

Rewrite as a division expression.

$$= 5(6)(2) \div 4$$

Replace r with 6 and s with 2.

$$= 60 \div 4 \text{ or } 15$$

Multiply. Then divide.

Exercises

ALGEBRA Evaluate each expression if $x = 10$, $y = 5$, and $z = 1$.

1. $x + y - z$

2. $\frac{x}{y}$

3. $2x + 4z$

4. $x(2 + z)$

5. $\frac{6y}{10z}$

ALGEBRA Evaluate each expression if $r = 2$, $s = 3$, and $t = 12$.

6. $2t - rs$

7. $\frac{t}{rs}$

8. $t(4 + r)$

9. $(t - 2s)7$

10. $\frac{5t}{(r+3)}$

1-4 Pre-Algebra Summer Skills**Properties of Numbers**

Properties of Addition and Multiplication In algebra, there are certain statements called properties that are true for any numbers.

Property	Explanations	Example
Commutative Property of Addition	$a + b = b + a$	$6 + 3 = 3 + 6$ $9 = 9$
Commutative Property of Multiplication	$a \cdot b = b \cdot a$	$4 \cdot 5 = 5 \cdot 4$ $20 = 20$
Associative Property of Addition	$(a + b) + c = a + (b + c)$	$(3 + 4) + 7 = 3 + (4 + 7)$ $14 = 14$
Associative Property of Multiplication	$(a \cdot b) \cdot c = a \cdot (b \cdot c)$	$(2 \cdot 5) \cdot 8 = 2 \cdot (5 \cdot 8)$ $80 = 80$
Additive Identity	$a + 0 = 0 + a = a$	$10 + 0 = 0 + 10 = 10$
Multiplicative Identity	$a \cdot 1 = 1 \cdot a = a$	$5 \cdot 1 = 1 \cdot 5 = 5$
Multiplicative Property of Zero	$a \cdot 0 = 0 \cdot a = 0$	$15 \cdot 0 = 0 \cdot 15 = 0$

Example 1

Is subtraction of whole numbers associative? If not, give a counterexample.

$$(9 - 4) - 2 \stackrel{?}{=} 9 - (4 - 2)$$

State the conjecture.

$$5 - 2 \stackrel{?}{=} 9 - 2$$

Simplify.

$$3 \stackrel{?}{=} 7$$

Simplify.

This is a counterexample. So, subtraction of whole numbers is not associative.

Example 2

Name the property shown by the statement.

$$15 \times b = b \times 15$$

The order of the numbers and variables changed. This is the
Commutative Property of Multiplication.

Exercises

1. State whether the following conjecture is true or false: The multiplicative identity applies to division also. If false, give a counterexample.

Name the property shown by each statement.

2. $75 + 25 = 25 + 75$

3. $2 \cdot (3 \cdot 4) = (2 \cdot 3) \cdot 4$

4. $14 \cdot 1 = 14$

5. $p \cdot 0 = 0$

1-4**Pre-Algebra Summer Skills***(continued)****Properties of Numbers***

Simplify Algebraic Expressions To **simplify** an algebraic expression, perform all possible operations. Properties can be used to help simplify an expression that contains variables.

Example**Simplify each expression.**

a. $(9 + r) + 7$

$$(9 + r) + 7 = (r + 9) + 7$$

Commutative Property of Addition

$$= r + (9 + 7)$$

Associative Property of Addition

$$= r + 16$$

Add 9 and 7.

b. $3 \cdot (x \cdot 5)$

$$3 \cdot (x \cdot 5) = 3 \cdot (5 \cdot x)$$

Commutative Property of Multiplication

$$= (3 \cdot 5) \cdot x$$

Associative Property of Multiplication

$$= 15x$$

Multiply 3 and 5.

Exercises**Simplify each expression.**

1. $24 + (x + 6)$

2. $3 \cdot (4a)$

3. $9 + (12 + c)$

4. $13d \cdot 0$

5. $(3 + f) + 17$

6. $11 + (m + 5)$

7. $(b + 0) + 7$

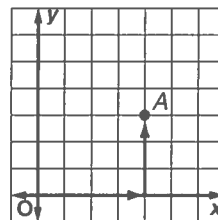
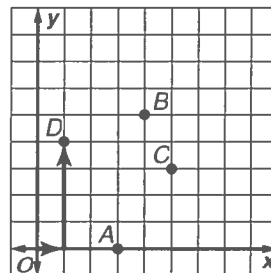
8. $15(a \cdot 1)$

9. $4w(6)$

10. $(n + 7) + 12$

1-6 Pre-Algebra Summer Skills**Ordered Pairs and Relations**

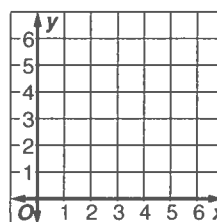
Ordered Pairs In mathematics, a **coordinate system** is used to locate points. The horizontal number line is called the **x-axis** and the vertical number line is called the **y-axis**. The point where the two axes intersect is the **origin** (0, 0). An **ordered pair** of numbers is used to locate points in the coordinate plane. The point (4, 3) has an **x-coordinate** of 4 and a **y-coordinate** of 3.

Example 1**Graph A(4, 3) on the coordinate plane.****Step 1** Start at the origin.**Step 2** Since the *x*-coordinate is 4, move 4 units to the right →.**Step 3** Since the *y*-coordinate is 3, move 3 units up ↑. Draw a dot.**Example 2****Write the ordered pair that names point D.****Step 1** Start at the origin.**Step 2** Move right → on the *x*-axis to find the *x*-coordinate of point D, which is 1.**Step 3** Move up ↑ the *y*-axis to find the *y*-coordinate, which is 4.

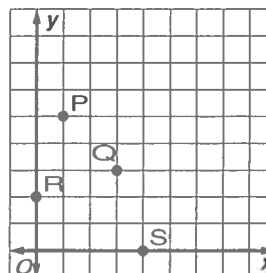
The ordered pair for point D is (1, 4).

Exercises**Graph each ordered pair on the coordinate plane.**

- | | |
|------------|------------|
| 1. A(4, 1) | 2. B(2, 0) |
| 3. C(1, 3) | 4. D(5, 2) |
| 5. E(0, 3) | 6. F(6, 4) |

**Refer to the coordinate plane shown at the right.****Write the ordered pair that names each point.**

- | | |
|------|-------|
| 7. P | 8. Q |
| 9. R | 10. S |



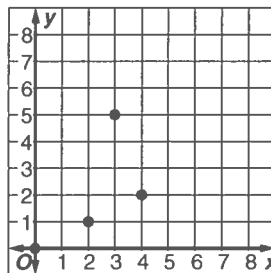
1-6 Pre-Algebra Summer Skills*(continued)***Ordered Pairs and Relations**

Relations A relation is a set of ordered pairs, such as $\{(0, 3), (1, 2), (3, 6), (7, 4)\}$. A relation can also be shown in a table or a graph. The set of x -coordinates is the **domain** of the relation, while the set of y -coordinates is the **range** of the relation.

Example

Express the relation $\{(0, 0), (2, 1), (4, 2), (3, 5)\}$ as a table and as a graph. Then determine the domain and range.

x	y
0	0
2	1
4	2
3	5



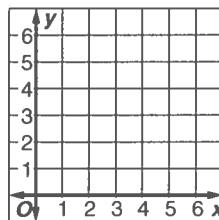
The **domain** is $\{0, 2, 4, 3\}$, and the **range** is $\{0, 1, 2, 5\}$.

Exercises

Express each relation as a table and as a graph. Then determine the domain and range.

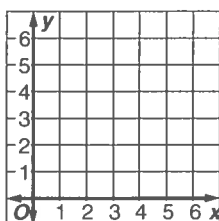
1. $\{(4, 6), (0, 3), (1, 4)\}$

x	y



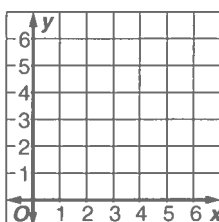
2. $\{(2, 5), (5, 3), (2, 2)\}$

x	y



3. $\{(1, 2), (3, 4), (5, 6)\}$

x	y



1-7 Pre-Algebra Summer Skills**Words, Equations, Tables, and Graphs**

Represent Functions Functions are relations in which each member of the domain is paired with *exactly* one member in the range. The function rule describes the operation(s) which must be performed on a domain value to get the corresponding range value. Function tables organize and display the input values (the x -coordinates), the function rule, and the output values (the y -coordinates).

Example

TICKETS June is ordering tickets for a show. Tickets cost \$22 each and there is a \$6 surcharge per order. Make a function table for 4 different input values and write an algebraic expression for the rule. Then state the domain and range of the function.

Step 1 Create a function table showing the input, rule, and output. Enter 4 different input values.

Step 2 The phrase “Tickets cost \$22 each and there is a \$6 surcharge per order” translates to $22x + 6$. Use the rule to complete the table.

Input (x)	Rule: $22x + 6$	Output (y)
1	$22(1) + 6$	28
2	$22(2) + 6$	50
3	$22(3) + 6$	72
4	$22(4) + 6$	94

Step 3 The domain is $\{1, 2, 3, 4\}$. The range is $\{28, 50, 72, 94\}$.

Exercises

For each ticket cost and surcharge given below, make a function table for 4 different input values and write an algebraic expression for the rule. Then state the domain and range of the function.

1. Ticket cost: \$8; surcharge: \$1.50

Input (x)	Rule:	Output (y)

Domain { }

Range { }

2. Ticket cost: \$12; surcharge: \$3

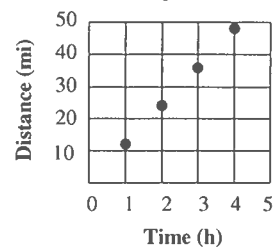
Input (x)	Rule:	Output (y)

Domain { }

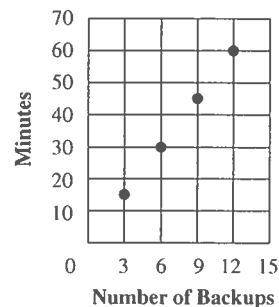
Range { }

1-7**Pre-Algebra Summer Skills***(continued)***Words, Equations, Tables, and Graphs****Multiple Representations** Functions can be described as words, equations, tables and graphs.**Words** The distance biked is equal to 12 miles per hour times the number of hours.**Equation** $d = 12t$ **Table**

Time (h)	Distance (mi)
1	12
2	24
3	36
4	48

Graph**Example****FILE PROTECTION** **Tori's computer backs up the file she is working on every 5 minutes. Make a function table to find the time for 3, 6, 9, and 12 backups. Then graph the ordered pairs.**Let m represent the number of minutes and b represent the number of backups. So, the rule is $m = 5b$.

Input (x)	$5b$	Output (y)
3	$5(3)$	15
6	$5(6)$	30
9	$5(9)$	45
12	$5(12)$	60

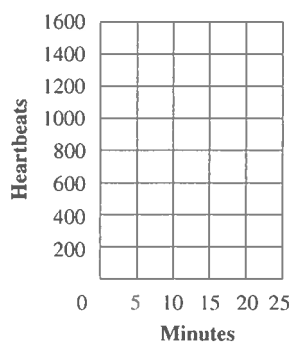
**Exercise**

1. Victor's heart beats 72 times a minute.

a. Write an equation to find the number of times Victor's heart beats for any number of minutes.

b. Make a function table to find the number of times Victor's heart beats in 5, 10, 15, and 20 minutes.

c. Graph the ordered pairs for the function.



Input (x)	Output (y)

2-1 Pre-Algebra Summer Skills***Integers and Absolute Value***

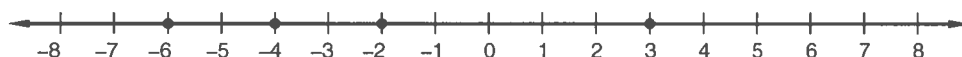
Compare and Order Integers The set of **integers** can be written $\{\dots, -3, -2, -1, 0, 1, 2, 3, \dots\}$ where \dots means *continues indefinitely*. Two integers can be compared using an **inequality**, which is a mathematical sentence containing $<$ or $>$.

Example 1 Write an integer for each situation.

- a. 16 feet below the surface

The integer is -16 .

- b. 5 strokes over par

The integer is $+5$ or 5 .**Example 2** Use the integers graphed on the number line below.Replace each \bullet with $<$, $>$, or $=$ to make a true sentence.

- a.
- $-6 \bullet -2$

-2 is greater since it lies to the right of -6 .
So write $-6 < -2$.

- b.
- $3 \bullet -4$

3 is greater since it lies to the right of -4 .
So write $3 > -4$.

Exercises**Write an integer for each situation.**

1. 2 inches less than normal

- 2.
- 13°F
- above average

3. a deposit of \$50

4. a loss of 8 yards

Replace each \bullet with $<$, $>$, or $=$ to make a true sentence.

5. $4 \bullet -4$

6. $8 \bullet 12$

7. $-7 \bullet -5$

8. $2 \bullet 5$

9. $-1 \bullet 1$

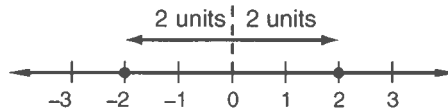
10. $4 \bullet -3$

11. $6 \bullet 8$

12. $-2 \bullet 12$

2-1**Pre-Algebra Summer Skills***(continued)****Integers and Absolute Value***

Absolute Value Numbers on opposite sides of zero and the same distance from zero have the same **absolute value**.

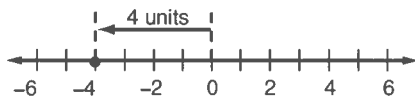


The symbol for absolute value is two vertical bars on either side of the number. $|2| = 2$ and $|-2| = 2$

Example 1**Evaluate each expression.**

a. $|-4|$

b. $|-3| + |6|$



$$|-3| + |6| = 3 + 6 = 9$$

$|-3| = 3$, $|6| = 6$
Simplify.

$|-4| = 4$

On the number line, -4 is 4 units from 0.

Example 2**Evaluate $|x| - 7$ if $x = -8$.**

$$\begin{aligned} |x| - 7 &= |-8| - 7 \\ &= 8 - 7 \\ &= 1 \end{aligned}$$

Replace x with -8.

The absolute value of -8 is 8.

Simplify.

Exercises**Evaluate each expression.**

1. $|-6|$

2. $|15|$

3. $|-12|$

4. $|21|$

ALGEBRA Evaluate each expression if $x = 8$ and $y = -3$.

5. $12 + |y|$

6. $x - |y|$

7. $2|x| + 3|y|$

2-2**Pre-Algebra Summer Skills*****Adding Integers*****Adding Integers
with the Same Sign**

Add their absolute values. The sum is:

- positive if both integers are positive.
- negative if both integers are negative.

Example 1**Find the sum $-3 + (-4)$.**

$$-3 + (-4) = -7$$

Add $|-3|$ and $|-4|$. The sum is negative.

**Adding Integers
with Different Signs**

Subtract their absolute values. The sum is:

- positive if the positive integer's absolute value is greater.
- negative if the negative integer's absolute value is greater.

Example 2**Find each sum.****a. $-5 + 4$**

$$\begin{aligned} -5 + 4 &= |-5| - |4| \\ &= 5 - 4 \text{ or } 1 \\ &= -1 \end{aligned}$$

Subtract $|4|$ from $|-5|$.

Simplify.

The sum is negative because $|-5| > |4|$.

b. $6 + (-2)$

$$\begin{aligned} 6 + (-2) &= |6| - |-2| \\ &= 6 - 2 \text{ or } 4 \\ &= 4 \end{aligned}$$

Subtract $|-2|$ from $|6|$.

Simplify.

The sum is positive because $|6| > |-2|$.

Exercises

Find each sum.

1. $6 + (-3)$

2. $-3 + (-5)$

3. $7 + (-3)$

4. $-4 + (-4)$

5. $-8 + 5$

6. $-12 + (-10)$

7. $6 + (-13)$

8. $-14 + 4$

9. $6 + (-6)$

10. $-15 + (-5)$

11. $-9 + 8$

12. $20 + (-8)$

2-2**Pre-Algebra Summer Skills***(continued)****Adding Integers***

Add More Than Two Integers Two numbers with the same absolute value but different signs are **opposites**. An integer and its opposite are also called **additive inverses**. This property is useful when adding 2 or more integers.

Additive Inverse Property

Words The sum of any number and its additive inverse is zero.

Example $5 + (-5) = 0$

Symbols $a + (-a) = 0$

Example**Find each sum.**

a. $-7 + (-16) + 7$

$$-7 + (-16) + 7 = -7 + 7 + (-16)$$

Commutative Property

$$= 0 + (-16)$$

Additive Inverse Property

$$= -16$$

Identity Property of Addition

b. $12 + (-4) + 9 + (-7)$

$$12 + (-4) + 9 + (-7) = 12 + 9 + (-4) + (-7)$$

Commutative Property

$$= (12 + 9) + [-4 + (-7)]$$

Associative Property

$$= 21 + (-11) \text{ or } 10$$

Simplify.

Exercises**Find each sum.**

1. $2 + 14 + (-2)$

2. $-8 + (-7) + 8$

3. $-13 + 11 + (-4)$

4. $7 + (-5) + (-6)$

5. $15 + 14 + (-12)$

6. $-9 + 17 + (-3)$

7. $24 + (-5) + 3$

8. $54 + 39 + (-54)$

9. $-42 + 20 + (-8)$

10. $-11 + (-6) + 22$

2-3**Pre-Algebra Summer Skills*****Subtracting Integers***

Subtracting Integers	To subtract an integer, add its additive inverse.
-------------------------	---

Example 1**Find each difference.****a. $9 - 17$**

$$\begin{aligned} 9 - 17 &= 9 + (-17) \\ &= -8 \end{aligned}$$

To subtract 17, add -17 .
Simplify.

b. $-7 - 3$

$$\begin{aligned} -7 - 3 &= -7 + (-3) \\ &= -10 \end{aligned}$$

To subtract 3, add -3 .
Simplify.

Example 2**Find each difference.****a. $4 - (-5)$**

$$\begin{aligned} 4 - (-5) &= 4 + 5 \\ &= 9 \end{aligned}$$

To subtract -5 , add $+5$.
Simplify.

b. $-6 - (-2)$

$$\begin{aligned} -6 - (-2) &= -6 + 2 \\ &= -4 \end{aligned}$$

To subtract -2 , add $+2$.
Simplify.

Exercises**Find each difference.**

1. $9 - 16$

2. $7 - 19$

3. $12 - 21$

4. $-5 - 3$

5. $-8 - 9$

6. $-13 - 17$

7. $7 - (-4)$

8. $9 - (-9)$

9. $-11 - (-2)$

10. $-6 - (-9)$

11. $-6 - 4$

12. $-16 - (-20)$

2-3**Pre-Algebra Summer Skills***(continued)****Subtracting Integers*****Evaluate Expressions** Use the rule for subtracting integers to evaluate expressions.**Example**

Evaluate each expression.

a. $x - 16$ if $x = 6$.

$$\begin{aligned}x - 16 &= 6 - 16 \\&= 6 + (-16) \\&= -10\end{aligned}$$

Write the expression. Replace x with 6.To subtract 16, add its additive inverse, -16 .Add 6 and -16 .**b. $a - b - c$ if $a = 7$, $b = 2$, and $c = -3$.**

$$\begin{aligned}a - b - c &= 7 - 2 - (-3) \\&= 5 - (-3) \\&= 5 + 3 \\&= 8\end{aligned}$$

Replace a with 7, b with 2, and c with -3 .

Use order of operations.

To subtract -3 , add its additive inverse, 3.

Add 5 and 3.

Exercises**ALGEBRA** Evaluate each expression if $a = 11$, $b = -1$, and $c = -8$.

1. $a - 14$

2. $b - 5$

3. $12 - c$

4. $33 - a$

5. $c - 8$

6. $-19 - b$

7. $-5 - c$

8. $3 - a$

9. $b - (-1)$

10. $a - (-7)$

11. $6 - b$

12. $c - (-12)$

2-4**Pre-Algebra Summer Skills*****Multiplying Integers***

Multiplying Integers with Different Signs	The product of two integers with different signs is negative.
--	---

Example 1**Find each product.**

a. $4(-3)$

$4(-3) = -12$

b. $-8(5)$

$-8(5) = -40$

Multiplying Integers with the Same Sign	The product of two integers with the same sign is positive.
--	---

Example 2**Find each product.**

a. $6(6)$

$6(6) = 36$

b. $-7(-4)$

$-7(-4) = 28$

Example 3**Find $6(-3)(-2)$.**

$6(-3)(-2) = [6(-3)](-2)$

$= -18(-2)$

$= 36$

Use the Associative Property.

$6(-3) = -18$

$-18(-2) = 36$

Exercises**Find each product.**

1. $-5(7)$

2. $6(-9)$

3. $-10 \cdot 4$

4. $-12 \cdot -2$

5. $5(-11)$

6. $-15(-4)$

7. $-14(2)$

8. $6(14)$

9. $-18 \cdot 2$

10. $-4(-4)(5)$

11. $6(-7)(2)$

12. $-10(-4)(-6)$

2-4**Pre-Algebra Summer Skills***(continued)****Multiplying Integers***

Algebraic Expressions Use the rules for multiplying integers to simplify and evaluate algebraic expressions.

Example 1 Simplify $-3a(-12b)$.

$$\begin{aligned}-3a(-12b) &= (-3)(a)(-12)(b) \\ &= (-3 \cdot -12)(a \cdot b) \\ &= 36ab\end{aligned}$$

$$\begin{aligned}-3a &= (-3)(a), -12b = (-12)(b) \\ \text{Commutative Property of Multiplication} \\ -3 \cdot -12 &= 36, a \cdot b = ab\end{aligned}$$

Example 2 Evaluate $4xy$ if $x = 3$ and $y = -5$.

$$\begin{aligned}4xy &= 4(3)(-5) \\ &= [4(3)](-5) \\ &= 12(-5) \\ &= -60\end{aligned}$$

$$\begin{aligned}\text{Replace } x \text{ with } 3, \text{ and } y \text{ with } -5. \\ \text{Associative Property of Multiplication} \\ \text{The product of } 4 \text{ and } 3 \text{ is positive.} \\ \text{The product of } 12 \text{ and } -5 \text{ is negative.}\end{aligned}$$

Exercises**ALGEBRA** Simplify each expression.

1. $9(-3w)$

2. $2e \cdot 9f$

3. $-8 \cdot 7m$

4. $-4s(-7)$

5. $10p(-5q)$

6. $n \cdot 6 \cdot 8$

ALGEBRA Evaluate each expression if $x = -4$ and $y = 8$.

7. $4x$

8. $3y$

9. $-12x$

10. $-6y$

11. xy

12. $-xy$

2-5**Pre-Algebra Summer Skills*****Dividing Integers***Dividing Integers
with the Same Sign

The quotient of two integers with the same sign is positive.

Example 1

Find each quotient.

a. $14 \div 2$

The dividend and the divisor have the same sign.

$14 \div 2 = 7$

The quotient is positive.

b. $\frac{-25}{5}$

$\frac{-25}{5} = -25 \div (-5)$

The dividend and divisor have the same sign.

$= 5$

The quotient is positive.

Dividing Integers with
Different Signs

The quotient of two integers with different signs is negative.

Example 2

Find each quotient.

a. $36 \div (-4)$

The signs are different.

$36 \div (-4) = -9$

The quotient is negative.

b. $-\frac{42}{6}$

The signs are different.

$-\frac{42}{6} = -7$

The quotient is negative.

Exercises

Find each quotient.

1. $32 \div (-4)$

2. $-18 \div (-2)$

3. $-24 \div 6$

4. $-36 \div (-2)$

5. $50 \div (-5)$

6. $-81 \div (-9)$

7. $-72 \div (-2)$

8. $-45 \div 3$

9. $-60 \div (-12)$

10. $-\frac{28}{2}$

11. $\frac{36}{-4}$

12. $\frac{-125}{-25}$

2-5**Pre-Algebra Summer Skills***(continued)****Dividing Integers***

Mean (Average) To find the mean, or average, of a set of numbers, find the sum of the numbers and then divide by the number of items in the set. Use the rules for dividing integers to find the mean.

Example

OCEANOGRAPHY The diving depths in feet of 7 scuba divers studying schools of fish were -12 , -9 , -15 , -8 , -20 , -17 , and -10 . Find the mean diving depth.

$$\frac{-12 + (-9) + (-15) + (-8) + (-20) + (-17) + (-10)}{7} = \frac{-91}{7}$$

Find the sum of the diving depths.
Divide by the number of divers.

$$= -13$$

Simplify.

The mean diving depth is -13 feet, or 13 feet below sea level.

Exercises

- 1. WEATHER** The low temperatures in degrees Fahrenheit for a week were -3 , 5 , -9 , 2 , 6 , -11 , and -4 . Find the mean temperature.

- 2. MONEY** The last 6 entries in Ms. Caudle's checkbook ledger show both deposits and withdrawals. Ms. Caudle wrote down \$100, $-\$20$, $-\$35$, \$250, $-\$150$, and $-\$85$. What is the mean dollar amount for these entries?

- 3. GOLF** During 5 rounds of golf, James had scores of 2 , -1 , 0 , -2 , and -4 . Find the mean of his golf scores.

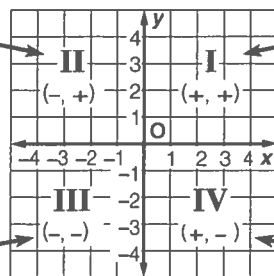
- 4. TRAINING** To train himself for a triathlon, Josh runs every day. Last week he ran 5 miles, 7 miles, 3 miles, 4 miles, 8 miles, 10 miles and 5 miles. What is the mean number of miles he ran last week?

2-6

Pre-Algebra Summer Skills

Graphing in Four Quadrants

The coordinates are
(negative, positive).



The coordinates are
(positive, positive).

The coordinates are
(negative, negative).

The coordinates are
(positive, negative).

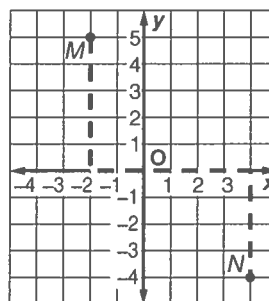
Example

Graph and label each point on a coordinate plane.

Name the quadrant in which each point lies.

a. $M(-2, 5)$

Start at the origin. Move 2 units left.
Then move 5 units up and draw a dot.
Point $M(-2, 5)$ is in **Quadrant II**.



b. $N(4, -4)$

Start at the origin. Move 4 units right.
Then move 4 units down and draw a
dot. Point $N(4, -4)$ is in **Quadrant IV**.

Exercises

Graph and label each point on the coordinate plane.

Name the quadrant in which each point is located.

1. $A(2, 6)$

2. $B(-1, 4)$

3. $C(0, -5)$

4. $D(-4, -3)$

5. $E(2, 0)$

6. $F(3, -2)$

7. $G(-4, 4)$

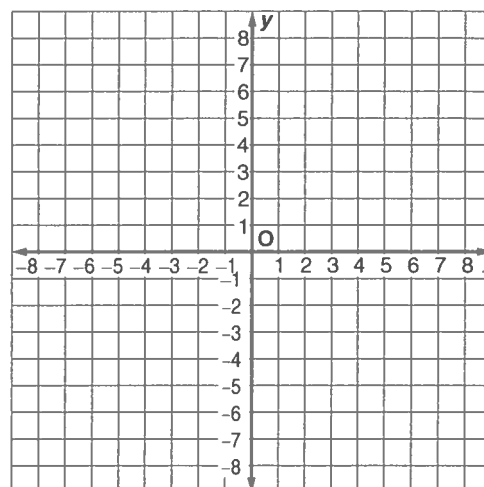
8. $H(2, -5)$

9. $I(6, 3)$

10. $J(-5, -8)$

11. $K(3, -5)$

12. $L(-7, -3)$



2-6 Pre-Algebra Summer Skills

(continued)

Graphing in Four Quadrants

Graph Algebraic Relationships A coordinate graph can be used to show relationships between two numbers.

Example

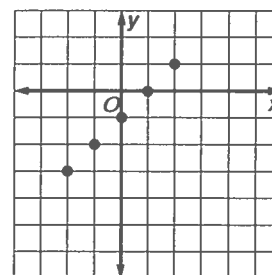
MONEY The difference between Zora's and Charlie's bank accounts is \$1. If x represents Zora's bank account and y represents Charlie's bank account, make a function table of possible values for x and y . Graph the ordered pairs and describe the graph.

Step 1 Make a table. Choose values for x and y that have a difference of 1.

Step 2 Graph the ordered pairs.

The points are along a diagonal line that crosses the x -axis at $x = 1$.

$x - y = 1$		
x	y	(x, y)
2	1	(2, 1)
1	0	(1, 0)
0	-1	(0, -1)
-1	-2	(-1, -2)
-2	-3	(-2, -3)

**Exercises**

- 1. TEMPERATURE** The sum of two temperatures is 3°F . If x represents the first temperature and y represents the second temperature, make a function table of possible values for x and y . Graph the ordered pairs and describe the graph.

$x + y = 3$		
x	y	(x, y)

